Experiments in Learning Prototypical Situations for Variants of the Pursuit Game

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Abstract

We present an approach to learning cooperative behavior of agents. Our approach is based on classifying situations with the help of the nearest-neighbor rule. In this context, learning amounts to evolving a set of good prototypical situations. With each prototypical situation an action is associated that should be executed in that situation. A set of prototypical situation/action pairs together with the nearest-neighbor rule represent the behavior of an agent.

We demonstrate the utility of our approach in the light of variants of the well-known pursuit game. To this end, we present a classification of variants of the pursuit game, and we report on the results of our approach obtained for variants regarding several aspects of the classification. A first implementation of our approach that utilizes a genetic algorithm to conduct the search for a set of suitable prototypical situation/action pairs was able to handle many different variants.

1 Introduction

Designing a set of agents and an organization and interaction scheme for them in order to solve a given problem cooperatively is not an easy task. Even if the designer does not have to cope with additional restrictions like the use of already existing software, interface restrictions, or also involved fellow designers, the task remains difficult and its realization is often very expensive.

Especially in cases where the designer is not familiar with the given problem, it can be expected that the first design (which is typically following well-known and quite general principles) has to be evolved over several versions until a satisfactory version is found. These versions reflect the learning and understanding process of the designer. The more versions are needed, the more expensive the task becomes.

An idea that has become more and more interesting and therefore a research goal of many computer scientists is to integrate learning and adaptation capabilities into the first design of agents in order to let them evolve the intended behavior automatically (and at much cheaper costs). The idea of providing an agent with learning capabilities, and using it as a start design for a range of problems has a strong potential, although some basic methods and representations concerning the problem domain should—not only in our opinion—be provided by a designer or a specialist of the domain. This concept is a basis for the growing field of genetic programming ([Ko91]), but also to some degree applies to areas like software engineering in form of software generators, or multi-agent systems as a means for the reuse of agents or multi-agent platforms.

In this paper we present an agent architecture based on the classification of situations with the nearest-neighbor rule (NNR; [CH67]), and a learning mechanism based on the generation of prototypical situations that demonstrate the utility of the idea to have agents adapt automatically to problems in order to evolve cooperative behavior.

The agents in our approach ground their behavior on a set of pairs of a situation and an action (sequence). When an agent is confronted with a situation it determines the situation/action pair in its set of situation/action pairs whose situation is the most similar to the given situation according to the NNR. Then it applies the action (sequence) associated with the selected pair. Since the behavior of such an agent can be easily changed by modifying, adding, or removing situation/action pairs, this architecture provides a suitable basis for learning and adaptation.

Learning cooperative behavior in this context means searching for an appropriate set of prototypical situation/action pairs. In order to realize this search, we have chosen a genetic algorithm (GA; [Ho92], [Jo88]) that allows us to start from rather inappropriate (unfit) sets, and without much knowledge besides an apt representation of situations and a comparison procedure for sets of situation/action pairs in order to determine the fitter set. This procedure is the basis for the fitness measure of the GA. We show the utility of our approach by learning agents for several different variants of the so-called pursuit game.

This paper is organized as follows: After this introduction we will describe in more detail our basic agent architecture. In section 3 we will concentrate on learning (satisfactorily) good cooperative behavior for agents. Then we will describe the pursuit game and its variants. In section 5 we will present the representation of the pursuit game

and its variants in terms of situations and actions, and the results of our experiments obtained with our approach for this game. Finally, we will conclude this paper with some remarks on possible improvements or alterations of our approach.

2 The Basic Agent Architecture

An agent exposed to some (multi-agent) environment has to repeat the process of taking some action A when being confronted with a certain situation S in order to continuously modify its situation so as to (finally) achieve some goal (as efficiently as possible). Commonly, a situation S is represented by a vector of n variables from the set \Re of real numbers. Hence, \Re^n is the set of all situations respectively the situation space. Each component x_i of a situation $S = (x_1, \ldots, x_n) \in \Re^n$ essentially expresses a certain feature of S. Given A as the set of all possible actions (respectively action sequences) an agent may take, the behavior of an agent is reflected by its strategy $\Psi : \Re^n \to A$ that allows the agent to select an action $\Psi(S) = A \in A$ when being confronted with situation S.

There are many ways to realize the behavior (strategy) of an agent, i.e., a mapping from \Re^n to \mathcal{A} . We propose here to utilize a finite, non-empty set $\mathcal{I} = \{(S_i, A_i) \in \Re^n \times \mathcal{A} \mid 1 \leq i \leq m_{\mathcal{I}}\}$ of prototypical situation/action pairs as basis for an agent's behavior. Given a situation $S \in \Re^n$, an agent takes the action A_j which is associated with the situation S_j —i.e., $(S_j, A_j) \in \mathcal{I}$ —that is closest (respectively the most similar) to S among all situations in \mathcal{I} . More precisely, we employ a distance measure \mathcal{D} : $\Re^n \times \Re^n \to \Re$ (typically the Euclidean distance measure that we also employed for our experiments). Given the minimal distance $\delta_{min} = \min(\{\mathcal{D}(S_i, S) \mid 1 \leq i \leq m_{\mathcal{I}}\})$ between situations S_i in \mathcal{I} and the given situation S, the action selected by strategy $\Psi_{\mathcal{I}}$ is $\Psi_{\mathcal{I}}(S) = A_j$, where $j = \min(\{1 \leq i \leq m_{\mathcal{I}} \mid \mathcal{D}(S_i, S) = \delta_{min}\})$ is the smallest index of situations in \mathcal{I} that are closest to S. (The smallest index is chosen merely to resolve ambiguities.)

Approaches based on the NNR fascinate with their simplicity. Nevertheless (or because of that) they have shown considerable success in connection with instance-based learning ([AKA91]) and classification problems (e.g. [MST94]). To our knowledge, all applications of the NNR involve a set \mathcal{I} which is (a subset of) a set of given training examples. (More recent work regarding classification problems, however, does not make such an explicit use of training examples. See for instance [DK95].)

We intend here to evolve the set \mathcal{I} with the help of a GA in order to optimize the performance of an agent proceeding according to strategy $\Psi_{\mathcal{I}}$. Since evolution can be equated with search, the GA is only one among many search methods that can be utilized. We chose the GA, because it has practical and theoretical properties that suit our approach (cp. section 3). Alternative search methods, in particular combinations of the GA with other search methods (using the TEAMWORK method ([De95]), for instance), can be investigated in future research (see also section 6).

Regardless of the search method employed, the basic architecture or design of a strategy determines (a) how good a strategy we can expect to find and (b) how difficult the search is going to be. Point (a) surely favors the use of neural nets, because a neural

net can realize (almost) any mapping provided that it is equipped with an apt topology and the connection weights are chosen appropriately (cp. [Sp65]). But evolving weight configurations and possibly also evolving net topology is a strenuous task even for the GA (cp. [ZM93]). Considering the fact that neural nets are "over-sophisticated" for many applications, simpler designs entailing more manageable search spaces are called for. Similar considerations apply to genetic programming.

Classifier systems ([Ho86], [Ho92]) can—by design—profit from the GA much more easily. Also, they are a very powerful methodology. But the rather complex architecture of a classifier system and the sophisticated techniques involved (e.g. credit assignment, bidding, etc.) still make it worthwhile thinking about simpler methods, in particular in connection with problems that do not require the full power of a classifier system.

The use of condition/action rules is a very popular approach in this context (e.g., [Gr91]). Commonly, such a rule is of the form

if
$$a_1 \leq x_1 \leq b_1 \wedge \ldots \wedge a_n \leq x_n \leq b_n$$
 then $execute \ A \in \mathcal{A}$,

where each condition $a_i \leq x_i \leq b_i$ specifies the range of values for variable x_i (with respect to this rule). In a set of rules, the rules are (implicitly) or-connected. Hence, such a set of rules can subdivide the situation space \Re^n into hyper-rectangles which are aligned with dimension axes. These hyper-rectangles may be partially overlapping, which calls for disambiguation techniques, and there may be gaps that necessitate some kind of default rules.

The major limitation of these condition/action rules is the restricted way they can subdivide the situation space. An approach based on a set of prototypical situation/action pairs and the NNR as described above allows for subdividing the situation space without overlapping and gaps, where the possible sub-spaces include, but are not limited to hyper-rectangles. As a matter of fact, such an approach can piecewise-linearly approximate arbitrary sub-space boundaries.

In [SS95], both approaches are combined. But the GA is only applied to evolve sets of condition/action rules, which then provide the NNR based component with situation/action pairs. We couple here the GA and the NNR approach tightly, meaning that the GA is immediately responsible for the set \mathcal{I} of situation/action pairs.

Before presenting the details of the GA designed for our approach, we would like to emphasize the simplicity of our approach: Once the situation space is known, the fundamental "data structure" is a situation respectively a point in the situation space and an associated action. Hence, the basic architecture of a strategy—namely a set of such situation/action pairs—is at least as easy to handle (by a GA) as a set of condition/action rules, though more expressive. No further user-specified knowledge is required as, for instance, non-terminals (functions) and terminals (constants, variables) in genetic programming.

3 Learning with the Genetic Algorithm

The preceding sections repeatedly pointed out that we intend to evolve respectively search for a strategy (behavior) $\Psi_{\mathcal{I}}$ respectively a finite set \mathcal{I} of situation/action pairs. So, the search space we have to cope with is the set of all finite sets of situation/action

pairs. Even if we limit the number of situation/action pairs of each set \mathcal{I} to some arbitrary but fixed $1 \leq M \in \mathbb{N}$, i.e., $m_{\mathcal{I}} \leq M$ for all $\mathcal{I} = \{(S_i, A_i) \mid 1 \leq i \leq m_{\mathcal{I}}\}$, the search space in general remains enormous (and unstructured). The use of a GA appears to be appropriate under these circumstances, because the GA has the potential to cope with intricate search spaces in the absence of any knowledge about their structure. Furthermore, a GA is less prone to getting trapped in a local optimum. Both properties are highly valuable for our purpose (cp. [JSG93]). In the sequel, we describe the basics of the GA in the light of our application.

Unlike other search methods, the GA maintains a set of (sub-optimal) solutions, i.e., several points in the search space. In this context, a solution is preferably called an individual, and the whole set is referred to as a population or generation. Usually, the size of the population is fixed. In order to explore the search space, the GA applies so-called genetic operators to (a subset of the) individuals of its current population. This way, new individuals can be created and hence new points in the search space can be reached. In order to keep the population size fixed, it must be determined which individuals are to be eliminated in order to make room for the new ones. For this purpose a so-called fitness measure is employed which rates the fitness (i.e., the ability to solve the problem at hand) of each individual of the current population. The genetic operators are applied to the most fit individuals, this way producing offspring which then replaces the least fit individuals (Darwinian principle of "survival of the fittest").

So, the GA basically proceeds as follows: Starting with a randomly generated initial population, the GA repeats the cycle comprising the rating of all individuals using the fitness measure, applying the genetic operators to (a selection) of the best individuals, and replacing the worst individuals with offspring of the best, until some termination condition is satisfied (e.g., an individual with a satisfactory fitness level has been created).

In our case an **individual** \mathcal{I} corresponds to a strategy represented by a (finite) set of situation/action pairs. (Our GA hence follows the 'Pittsburgh approach' in that each individual encodes a complete "solution" of the problem.) The **fitness** of an individual is assessed in terms of the problem solving expertise of its associated strategy $\Psi_{\mathcal{I}}$. The fitness measure is the only connection between the GA as an underlying search method and the actual problem. Therefore, we cannot define a specific fitness measure at this point, and we have to postpone details until a concrete problem is specified (see section 5).

The initial population of the GA is (as usual) generated completely at random. That is, for each individual \mathcal{I} of the initial population comprising n_{pop} individuals, both its size $m_{\mathcal{I}} \leq M$ and the $m_{\mathcal{I}}$ situation/action pairs are determined at random.

Two **genetic operators** are employed here, namely crossover and mutation. ('Reproduction' as given by [Ko91], for instance, is basically realized by the survival of the r% fittest individuals.) Offspring is produced through crossover, while mutation can modify this offspring.

The **crossover operator** randomly selects two distinct parents from the pool of r% best (surviving) individuals. A subset of the situation/action pairs of each parent individual is chosen at random, and the union of these two subsets yields the "child" individual. (Note that the surviving individuals here simply all have an equal chance

to become reproductive.) Thus, this operator complies with the basic idea of crossover, namely providing the ability to combine good partial solutions. Furthermore, the GA is supported by the modularity of individuals: Subsets of individuals actually can often be good partial solutions, e.g., for sub-problems occurring at early or final stages of the problem solving process, because a subset of situation/action pairs that work well for certain stages of the problem solving process will also function for these stages when being isolated. (The lack of modularity is the major problem GAs encounter in connection with Neural Networks. Interactions in a connectionist network are so close and intertwined that the ability to solve a certain sub-problem can hardly be accredited to a subset of the connection weights or parts of the whole network.)

The **mutation operator** modifies individuals stemming from crossover before they are admitted to the next generation. An individual \mathcal{I} is subject to mutation with probability P_{mut} . If an individual \mathcal{I} actually is selected for mutation, each situation/action pair of \mathcal{I} is—with probability P_{rnd} —replaced by a randomly generated situation/action pair. This operator introduces—controlled by the probabilities P_{mut} and P_{rnd} —random influences which are an essential ingredient of the GA.

4 The Pursuit Game and Some Variants

In order to demonstrate the potential of our approach to learning cooperating agents we need problems that require different degrees of cooperation and different behavior of agents. But these problems also have to be easy to understand (which does not imply that they can be solved easily as well), and should allow for comparisons regarding several criteria, e.g., complexity, necessary cooperation or solubility. Therefore it would be best to have one basic problem that allows for variants regarding several aspects.

Fortunately, there is such a basic problem, namely the so-called *pursuit game* (also called "hunter and prey") that was first presented in [BJD85]. Since then, a number of quite different approaches to solving this basic problem (see, for example, [Si90], [LR92]) and also some variants (see [GR+89], [SM89], [SM90]) have been proposed, so that the pursuit game can be called the "blocks world" of the DAI community.

The basic problem can be described as follows: There are four hunter agents (also called predators) and a prey agent on an infinite rectilinear grid. The game is played in discrete time steps. At each time step, an agent can move one square in a horizontal or vertical direction, or stay put. The prey selects its steps randomly. The hunters win the game, if they can surround the prey. No two agents may occupy the same square. The task is to develop a strategy for the hunters that enables them to win the game.

There are several aspects of this basic scenario that can be varied to obtain variants of the game. Such aspects are, for example, the number of hunters, the boundaries of the grid world, or the communication and observation capabilities of the agents. In the following we will take a closer look at all the aspects and the possible forms of these aspects. Then we will examine more closely some combinations of several aspects that either have been investigated in literature or will be investigated in section 5.

1. The form of the grid

In the basic scenario the grid-world has no boundaries and there are no obstacles

in it. Consequently, variants of this aspect are a grid-world with boundaries, for example a $N \times N$ grid, a world with no boundaries but some obstacles in it, or a world with boundaries and obstacles. The obstacles may have a certain regular shape or can have any shape.

2. The individual hunter

In the basic scenario a hunter agent does not have many features. Therefore one can obtain variants with respect to the following sub-aspects:

a) Shape and size

A hunter may not only occupy one square of the grid, but several of them. It may be quadratic, but it can also have other shapes.

b) Possible moves and actions

Besides moving only in the vertical or horizontal direction (or not moving at all) variants can include diagonal moves or turns (rotations), if turns actually have an effect. There can also be communication actions (see d)).

c) Speed

A hunter does not have to be as quick as the prey. It can be faster, for example two or three moves per time step, but it can also move more slowly than the prey, for example one move every two or three time steps.

d) Perception and communication capabilities

An aspect that greatly influences the strategy of a hunter (and therefore each solution attempt for the game) are its perception and communication capabilities. (Note that being able to see the other hunters is a kind of visual communication.) The spectrum of this aspect ranges from hunters that can neither communicate with nor see other hunters, over hunters that cannot explicitly communicate with the others but at least know their positions (which means that they have to cooperate without communication, see [RGG86]), and over hunters that cannot see each other, but can communicate, to hunters that both see their colleagues and are also able to send and receive messages.

e) Memory capabilities

An aspect that can become important if the hunters are able to communicate with each other is the memory of an agent. Memory allows an agent to remember plans and intentions of other hunters. There may be no memory, a restricted size for the memory, or an arbitrary amount of memory.

3. The hunting team

For most variants of the game more than one hunter (and cooperation between the hunters) are required so that there is a chance to succeed. Therefore, the composition of the team of hunters is also an aspect that can be varied.

a) The number of hunters

For each combination of the other aspects there is a minimal number of hunters needed to win the game. Deploying more hunters may help to win the game, but may also require different, possibly more sophisticated strategies and more effort in developing these strategies.

b) The type of the hunters
Since there can be different types of hunters (according to aspect 2), quite
different strategies—depending on what kind of hunters form the team—are
needed to cooperate in order to win the game.

4. The prey

The prey is an agent like the hunters. Therefore the same sub-aspects a) to e) apply with the exception that communication is only necessary if there are several prey agents (as was suggested in [MC93]). But there is an additional sub-aspect:

f) The strategy of the prey
The (escape) strategy of the prey is the main factor determining the difficulty
to win the game. Strategies range from simply moving in one direction
(which can be quite successful, see [HS+95]) over random moves to elaborate
strategies like maximizing the distance from the nearest or all hunters. Even
learning strategies to counter those of the hunters was suggested and tried
out (with perhaps too much success, see [HS+95], again).

5. The start situation

The start positions of both hunters and prey can also influence both the possibility to win the game and the effort for learning a cooperative strategy for the hunters. If the game is always started from the same positions and no random element is introduced by other aspects, then a winning strategy will always win (and is easier to learn). Otherwise, different start situations will lead to different outcomes.

6. The goal

Even for the definition of if and when the game is won there are two variants. The main question is to "capture" or to "kill". The prey is captured if it cannot move to another square anymore (i.e., it is totally surrounded by boundaries, obstacles and hunters). It is killed if the prey and a hunter occupy the same square (at some point in time). The goal may also include resource limitations.

For describing an actual variant of the pursuit game it is necessary to choose one of the possible instantiations for each aspect and sub-aspect. Obviously, the possibilities to win are quite different for different variants. While a prey that moves always in one direction on a grid-world without boundaries and obstacles will always escape the hunters if the start situation places all hunters on the wrong side of the prey and all agents have the same speed, there are also many variants for which successful strategies for the hunters can be found, provided the hunters are granted a sufficient number of moves (see section 5).

Most of the work regarding the pursuit game so far centered on strategies for particular variants that were developed by human beings, naturally with some emphasis on the cooperation (using communication) of the hunters. In [SM89] and [SM90] the authors concentrated on communication-intensive strategies for the hunters. Diagonal moves were presented in [Ko92]. (See also [Os95].)

But variants of the pursuit game were also used as a testbed for approaches to learning cooperative agents. In [HS+95] a genetic programming approach was applied to variants originating from variations of the escape strategy of the prey. Even experimental data concerning a co-evolution of hunters and prey was provided. Genetic programming results in programs that are more expressive than our approach, but more expertise on the parts of the designer is required, because not only a suitable representation of situations must be found, but also the building blocks of programs (functions and terminals) must be chosen properly.

Another work dealing with learning cooperative behavior and the pursuit game is described in [MC93]. There, a genetic algorithm approach was chosen to learn strategies for variants with n + 4 hunters and n prey agents (where n was varying). In contrast to our approach, in [MC93] a genetic algorithm is used to search good parameters for a program that includes memory and planning functions. Therefore, this approach does not provide such a high level of abstraction as our situation/action pairs.

5 Experiments

This section documents the experimental setting and the results we obtained with our approach to learning successful and cooperative strategies for the hunters for several variants of the pursuit game. In order to describe the setting we have to describe how to represent situations, actions, and—for the learning part—we describe the fitness measure ϑ of the GA.

5.1 The Representation of Situations and Actions

The representation of situations is the main factor that determines whether suitable agent strategies can be learned, how good they will be, and how difficult the learning and adaptation process will become. Clearly, there are different representations even for one variant of the pursuit game, and also clearly we have to expect that different variants need quite different representations. In fact, the representation is the only possibility for a designer to influence the evolving strategy (which was exactly our goal).

In our experiments we have chosen to use representations for situations that differ as little as possible from variant to variant (which kind of emulates an unexperienced designer and puts quite a burden on our learning approach). Due to this reason (but also due to the efficiency of our implementation that can only be seen as a first, very crude version) we restricted our experiments to only a few of the aspects of section 4. These aspects are the strategy of the prey, the start situation, the goal, the number of hunters, the possible moves, and the perception capabilities of the hunters.

All other aspects were fixed: There is just one prey. All $k \geq 1$ hunters are of the same type, i.e., they occupy one square, have the same possible moves, move at the same speed as the prey (one move per time unit), and have no memory capabilities. The prey always knows the position of all hunters, and in most experiments we used a 30×30 grid. Furthermore, we decided to have all hunters use the same strategy $\Psi_{\mathcal{I}}$ (which

is reasonable because the hunters are not distinguishable). Thus, learning amounts to searching for one suitable set \mathcal{I} of prototypical situation/action pairs.

Our basic representation of a situation is based on the positions of the agents regarding a distinguished reference square (0,0) employing the usual Cartesian coordinate system. Hunter i occupies square $(x_i, y_i) \in \mathbb{Z} \times \mathbb{Z}$, and the prey occupies square $(x, y) \in \mathbb{Z} \times \mathbb{Z}$. (\mathbb{Z} is the set of all integers.) We characterize the situation of hunter i with the help of its relative positions regarding prey and fellow hunters. That is, the situation S_i of hunter i is a vector consisting of $x - x_i$, $y - y_i$ and $x_j - x_i$, $y_j - y_i$ for $1 \le j \le k$ ($i \ne j$), the latter sorted according to j. If the hunters can see only the prey, then S_i merely is the tuple $(x - x_i, y - y_i)$. Hence, the situation space is \mathbb{Z}^{2k} , or \mathbb{Z}^2 if the hunters see only the prey.

This representation can be enhanced with hunter types, hunter orientation (if it is not quadratic), coordinates of obstacles, and memory fields (for more information about other hunters or for history information). The possible moves for both hunters and prey are either N, S, E, W or stay put, or these moves plus the diagonal moves NE, NW, SW, and SE. (If communication actions are possible, they also have to be added.) Hunters and prey execute their moves simultaneously. If a move is not possible (e.g., because another agent will occupy the target square or a boundary is reached), then the agent stays put.

As in the original pursuit game, no two hunters may occupy the same square. Conflicts are resolved by giving priority to hunter i over hunter j if i < j, unless of course hunter j holds its position (i.e., stays put), in which case any hunter that wants to move to that square is itself forced to stay put. If the objective of the hunters is to capture the prey by surrounding it, then they are also not allowed to move onto the square occupied by the prey. Conflict resolution involving the prey is realized by considering the prey as hunter 0, and then proceeding as described above.

On a $N \times N$ grid, \mathbb{Z} can be restricted to $\mathbb{Z}_N = \{-N+1, \ldots, N-1\}$. Hence, in order to produce random situations, random numbers from \mathbb{Z}_N are generated. But also on an infinite grid this restriction makes sense not only for practical reasons: Prototypical situations are more likely to appear (more frequently) near the crucial end of the hunt where hunters and prey are close together, i.e., near situation $(0,\ldots,0)$. For this very reason we refrained from generating random numbers that are distributed equally in \mathbb{Z}_N , but instead produced random numbers that are biased towards 0. To this end, we generated random numbers $x \in [0;1[$, and created the bias by using x^e , $e \geq 1$ (e = 1.5 in our experiments). We then obtained random numbers $z \in \mathbb{Z}_N$ by using either $z = |x^e \cdot N|$ or $z = -|x^e \cdot N|$, where both alternatives are equally probable.

In our experiments, the possible instantiations for the varying aspects are: The hunters either see each other and the prey, or only the prey. The start situation is either fixed (prey in the center of the 30×30 grid, hunters lined up along the whole western boundary with equal distance from each other; a single hunter starts from the middle of the boundary), or chosen at random (prey in the center, each hunter at least 5 squares away from it in both horizontal and vertical direction). These start positions are also used in case of an infinite grid, but naturally the grid boundaries are ignored after setting up the initial situation. The goal situations are killing or capturing the prey. The number of hunters is the minimal number that is required to win the game

(theoretically). There will also be some remarks on the effect of additional hunters in subsection 5.3.

Finally, there are five escape strategies Φ_1, \ldots, Φ_5 . Note that, to our knowledge, Φ_4 and Φ_5 are novel, and that in particular Φ_5 proved to be quite challenging (cp. subsection 5.3). Besides precluding moves that violate some rules or restrictions, the prey also does not consider moves that lead to a square currently occupied by a hunter, although the hunter might move away from that square. The remaining moves are referred to as eligible moves. Each escape strategy (except for Φ_2) centers on a different vector of distance values $(d_1, \ldots, d_m), m \geq 1$, that reflects the current situation of the prey from a certain point of view. Common to all these strategies is that the prey tries out (simulates) all eligible moves and then picks the best move (tested first). Distance vectors are compared using the usual lexicographic ordering $>_{lex}$ (left-to-right comparison with >), where "greater" means "better". If diagonal moves are allowed, then the basic distance measure is the Euclidean distance. The "Manhattan distance" is employed otherwise. In the sequel, let \hat{d}_i be the basic distance between prey and hunter i.

- Φ_1 : Maximize distance from nearest hunter: $m = 1, d_1 = \min(\{\hat{d}_1, \dots, \hat{d}_k\})$.
- Φ_2 : Random movement: Among all eligible moves the prey chooses one move at random. Staying put is not an eligible move here. Consequently, the prey does not stay put unless trapped.
- Φ_3 : Maximize sum of distances from all hunters: $m=1, d_1=\hat{d}_1+\cdots+\hat{d}_k$.
- Φ_4 : Maximize vector of sorted distance values: $m = k, (d_1, \ldots, d_k)$ is obtained by sorting $\hat{d}_1, \ldots, \hat{d}_k$ so that $d_i \leq d_{i+1}$.
- Φ_5 : Escape strategy Φ_5 is an extension of Φ_4 . In addition to $\hat{d}_1, \ldots, \hat{d}_k$, the prey here also takes into account its smallest distance from each of the four grid boundaries. Consequently, m = k + 4. By also trying to maximize the distance from grid boundaries, escape strategy Φ_5 alleviates a "flaw" of escape strategy Φ_4 which (like Φ_1 and Φ_3) essentially makes the prey run away to some grid boundary where it can be captured or killed much more easily than it can be when trying to stay in "open field" as long as possible. (Obviously, Φ_5 cannot be applied in connection with an infinite grid-world.)

5.2 The Fitness Measure ϑ

The fitness measure ϑ is to rate the performance of an individual \mathcal{I} , i.e., a set of situation/action pairs. The performance of \mathcal{I} is given by the suitability of the associated strategy $\Psi_{\mathcal{I}}$ employed by each hunter. In case random effects can occur, it is clear that the fitness cannot be determined reasonably based on merely one trial (hunt). Consequently, several trials have to be executed, and the outcomes of these elementary fitness values must be combined to obtain the overall fitness ϑ .

The elementary fitness measure θ rates a single trial. θ should therefore reflect if the hunters were successful in that particular trial, and in that case, how fast they

succeeded. In case of failure, θ should somehow express how close to success the hunters came. Naturally, the hunters cannot be granted an arbitrary amount of time. If they do not succeed within T=200 time steps, then their hunt is judged a failure.

The elementary fitness measure $\theta(\mathcal{I}) \in \mathbb{N}$ is defined as follows.

$$\theta(\mathcal{I}) = \begin{cases} t_s, & \text{success in } t_s \leq T \text{ time steps} \\ \sum_{t=1}^T \sum_{i=1}^k \delta(i, t), & \text{in case of failure,} \end{cases}$$

where $\delta(i,t)$ is the Manhattan distance that separates hunter i from the prey at time step t. Hence the elementary fitness $\theta(\mathcal{I})$ is the smaller the fitter \mathcal{I} is considered to be.

The overall fitness $\vartheta(\mathcal{I})$ of \mathcal{I} is computed in a straight forward way on the basis of $b \geq 1$ trials which result in b elementary fitness values $\theta_1(\mathcal{I}), \ldots, \theta_b(\mathcal{I})$:

$$\vartheta(\mathcal{I}) = \frac{1}{b} \cdot \sum_{i=1}^{b} \theta_i(\mathcal{I}).$$

If no random effects occur, we set b=1, and b=20 else. An individual \mathcal{I} is considered as being successful only if all b trials were successful. If two individuals have the same overall fitness measure, then the more concise individual containing less situation/action pairs is preferred.

For our experiments, the parameters of the GA were chosen as follows (cp. section 3): r = 30%, $P_{mut} = 50\%$, $P_{rnd} = 10\%$, $n_{pop} = 100$. The maximal number M of situation/action pairs of an individual \mathcal{I} was restricted to 30. (All these settings were determined after a few preparatory experiments and are in no sense "optimal".) The maximal number of generations (cycles) of the GA was limited to 100. The GA stopped before exceeding this limit as soon as a successful individual was found.

For each variant of the pursuit game the GA was run 5 times, and the performance of the best individual that surfaced in (one of) these 5 runs is presented. This 'best-of-5' policy is reasonable, because (not only our) experiments corroborated that several shorter runs are more promising than a single run (cp. [Ko91]).¹

5.3 Results

Tables 1-4 present the core of our experimental results in connection with a 30×30 grid. (We will also report on other experiments that do not fit into these tables.) Each table and its caption specify the particular variant of the pursuit game. The column labeled with 'k' shows the number of hunters. The columns labeled with 200, 1000, 10000 display the performance of the 'best-of-5' individual when granted the respective number T of time steps. (Note that T=200 during learning.) The performance is given as the number of steps necessary to succeed if no random effects can occur. Otherwise, a success rate is given that was determined based on 100 trials.

Being granted more time steps T only pays off in connection with random escape strategy Φ_2 . There, the hunters essentially chase the prey, waiting for the prey to make a certain sequence of moves that allows them to succeed. Naturally, the probability for

¹We picked the number '5' more or less arbitrarily.

Table 1: Hunters see only the prey, and their objective is to "kill".

	Fixed Start Positions									Random Start Positions								
	No Diagonal Moves Diagonal Moves							No Diagonal Moves				Diagonal Moves						
Φ	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000		
Φ_1	2	33	33	33	2	28	28					100%						
Φ_2	1	100%	100%	100%	1	100%	100%	100%	1	96%	99%	100%	1	99%	100%	100%		
Φ_3	2	28	28	28	2	28	28	28	2	100%	100%	100%	2	100%	100%	100%		
Φ_4	2	44	44	44	2	28	28	28	2	100%	100%	100%	2	99%	99%	99%		
Φ_5	2	54	54	54	2	26	26	26	2	99%	99%	99%	2	100%	100%	100%		

Table 2: Hunters see only the prey, and their objective is to "capture".

			Fixe	d Start	P	ositie	ons		Random Start Positions									
	No Diagonal Moves Diagonal Moves							N	No Diagonal Moves Diagonal Mo									
Φ	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000		
Φ_1	2	56	56	56	3	28	28	28	2	100%	100%	100%	3	96%	96%	96%		
Φ_2	2	55%	100%	100%	3	5%	22%	72%	2	10%	81%	100%	3	3%	37%	92%		
Φ_3	2	56	56	56	3	28	28	28	2	0%	0%	0%	3	100%	100%	100%		
Φ_4	2	59	59	59	3	33	33	33	2	0%	0%	0%	3	88%	88%	88%		

this to happen increases with the number of time steps. However, by allowing diagonal and hence more moves, this probability decreases, which is reflected by the sometimes significant worse performance of the hunters when dealing with a prey using Φ_2 and diagonal moves compared to the case where no diagonal moves are allowed.

For all other strategies, failure is almost always caused by some kind of "deadlock" (e.g., the hunters chase the prey around in circles), so that increasing T does not improve the success rate. Diagonal moves here, however, are profitable for the hunters. They allow the hunters to approach the prey faster and, if the prey is sitting in a corner of the (finite) grid, they can approach it in a way so that the prey will not try to escape, because none of its alternatives improves its situation (in terms of distance from hunters). "Killing" can become very easy under these circumstances. In particular if the prey employs Φ_3 , a successful strategy (possibly consisting of merely one situation/action pair) can often be found in the initial random population.

Tables 1 and 2 show that the theoretically minimal number of hunters² almost always suffice to succeed respectively to achieve an acceptable success rate (if granted sufficient time) even though the hunters only focus on the prey (emergent behavior). The only significant failure (0% success rate) occurs when 2 hunters starting from random positions attempt to capture the prey that tries to escape using either Φ_3 or Φ_4 , and diagonal moves are not allowed (see table 2). If 3 hunters are deployed, the success rate is close to 100% in both cases.

²If hunters focus on both prey and fellow hunters, we always deploy $k \geq 2$ hunters.

Table 3: Hunters see both prey and fellow hunters, and their objective is to "kill".

	Fixed Start Positions									Random Start Positions								
	No Diagonal Moves Diagonal Moves								No Diagonal Moves					Diagonal Moves				
Φ	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000		
Φ_1	2	29	29	29	2	28	28	28	2	100%	100%	100%	2	100%	100%	100%		
Φ_2	2	100%	100%	100%	2	99%	100%	100%	2	96%	100%	100%	2	100%	100%	100%		
Φ_3	2	28	28	28	2	28	28	28	2	78%	78%	78%	2	98%	98%	98%		
Φ_4	2	42	42	42	2	28	28	28	2	82%	82%	82%	2	99%	99%	99%		
Φ_5	2	182	182	182	2	26	26	26	2	74%	74%	74%	2	100%	100%	100%		

Table 4: Hunters see both prey and fellow hunters, and their objective is to "capture".

	Fixed Start Positions									Random Start Positions								
	No Diagonal Moves					Diagonal Moves								Diagonal Moves				
Φ	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000	k	200	1000	10000		
Φ_1	2	56	56	56	3	30	30					83%						
Φ_2	2	53%	100%	100%	3	4%	18%	88%	2	50%	100%	100%	3	1%	3%	21%		
Φ_3	2	57	57	57	3	28	28	28	2	11%	11%	11%	3	81%	81%	81%		
Φ_4	2	61	61	61	3	28	28	28	2	99%	99%	99%	3	81%	81%	81%		

From a theoretical point of view it is clear that hunters that see both prey and fellow hunters are at least as versatile as hunters that see only the prey. But taking into account fellow hunters enlarges the situation space and thus complicates the search space. This is the main reason why we sometimes obtained worse results in practice although better results have to be expected in theory.

Nonetheless, considering fellow hunters sometimes leads to significant improvements (possibly because it is indispensable). This happened, for instance, in connection with the case discussed above where 2 hunters focusing on the prey had a success rate of 0%; 2 hunters that also see each other performed significantly better (cp. tables 2 and 4). We could make this observation again when tackling a variant related to the original version of the pursuit game. Only 4 hunters hunting a prey using Φ_2 on an infinite grid that see each other achieved an acceptable success rate (55% when being granted 10000 time steps and starting from fixed positions).

Furthermore, a prey using the quite sophisticated escape strategy Φ_5 appears to be very hard to capture. First of all, a prey using Φ_5 tries to stay away from boundaries and corners. As a matter of fact, it cannot be forced to move into a corner or next to a boundary in any way. Consequently, 4 hunters are required to capture the prey if diagonal moves are not allowed (8 hunters else). In our experiments, 4 hunters only succeeded when they knew about their fellow hunters. Additionally, we had to refine the (elementary) fitness measure in order to penalize passivity, because very often "almost successful" strategies evolved that made the hunters move very close to the prey (without capturing it) and then stop there. Since the prey also stayed put, the

strategy received a fitness measure that was better than the one a more "aggressive" strategy got. (Moving closer made the prey run away.) We avoided these local optima by adding the number of time steps the hunters were passive to the elementary fitness value. (Recall that a higher fitness value means worse fitness.) The GA then found a successful strategy that allowed 4 hunters to capture the prey after 104 time steps (fixed start situation).

We also examined the effects a surplus of hunters can have. On the one hand, it is understandable that more hunters have a better chance to win the game. On the other hand, due to the fitness measure, all hunters will chase the prey and hence might hinder each other, in particular when they only focus on the prey. (In order to favor more sophisticated pursuit strategies involving "driving" and "ambushing" the fitness measure has to be adapted appropriately.) In our experiments, increasing the number of hunters (up to 7) did not have any significant negative effects (except for complicating the search space if fellow hunters were to be considered, of course).

The time spent by the GA to process an entire generation ranged between 0.5 and 1 second, if the number of trials b = 1 (10-20 seconds if b = 20). (Run times were obtained on a SPARCstation 20.) These numbers refer to the case where the situation space is \mathbb{Z}^2 . If the situation space is \mathbb{Z}^{2k} , k > 1, then the run times increase linearly with k. (This increase is quite small. E.g., for k = 2, a generation can still be processed in about 1 respectively 20 seconds.)

If the task of the hunters was rather easy, then a successful strategy $\Psi_{\mathcal{I}}$ (respectively a set \mathcal{I} of situation/action pairs) was found within 15 generations. For harder tasks (in particular capturing a prey that employs Φ_2), the maximal number of generations (100) was sometimes exceeded. The number of situation/action pairs of a successful individual \mathcal{I} covered the whole spectrum from 1 to 30 (mostly around 20). This number seems to be quite arbitrary, which is understandable, because the GA stopped as soon as the first successful \mathcal{I} was found. By having the GA continue, the number of situation/action pairs can decrease significantly. (Recall that parsimony is a secondary fitness criterion.)

Finally, we cannot discuss here the full variety and the peculiarities of the learned hunter strategies. But one observation is worth mentioning: Given a random start situation and a non-random escape strategy, in the majority of cases the hunters at some point in time reached a situation from where they then always proceeded the same way. Such a behavior makes sense, because the final phase of a hunt is much more tricky than the initial approach phase. Therefore, it is sensible and much easier to focus on a certain kind of final phase and to attempt to reach a situation from where this final phase can start. This resembles the behavior of many human beings.

6 Discussion

We have presented an approach for learning cooperative behavior of reactive agents that is based on the search for a set of prototypical situation/action pairs. An agent employs the nearest-neighbor rule to select that pair whose prototypical situation is closest (most similar) to the actual situation, and then performs the associated action.

In our current implementation, the search is conducted by a genetic algorithm.

Our goal was to demonstrate that this approach is considerably versatile in that it allows a designer of multi-agent systems to specify requirements on a very high level in terms of a representation of situations and possible actions (and a comparison of strategies in our case), and then a satisfactory solution is evolved automatically. We could show that this goal can be achieved in many cases: We presented aspects of the well-known pursuit game that can be varied so as to obtain variants of the game, and for many of these (non-trivial) variants the first implementation of our approach succeeded in evolving apt strategies.

However, our experiments also suggested several improvements. Although it was surprising how well our ad hoc implementation of the genetic algorithm performed, for problems involving a more complex representation of situations improvements are necessary. The use of additional knowledge (apart from the knowledge integrated with the fitness measure), alternative search methods (possibly combined with the genetic algorithm), and enhanced efficiency through distributed search seem to be profitable. The TEAMWORK approach to distributed search ([De95]) is capable of achieving these goals, nevertheless providing a high level of abstraction for the designer.

A comparison of our approach with other (learning) approaches in connection with the pursuit game is at the time rather difficult, because other approaches mostly have been examined with respect to a few particular variants of the game. Moreover, in most cases the experimental setting cannot be reproduced, because full information on all aspects of the game is not available. But this is essential in order to obtain a reliable comparison, because (as our experiments have shown) tiny variations of the setting can have significant effects.

Finally, our approach has been successfully employed for obtaining optimized nearest-neighbor classifiers based on generated instances ([FA96]). Unlike common approaches based on the nearest-neighbor rule, the given set of training instances is only used to measure the fitness of a classifier that employs a set of instances evolved by our approach. (Situations correspond to the attribute vectors describing the objects to be classified, and actions correspond to classes.)

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